## [Contribution from the Pittsburgh Experiment Station, U. S. Bureau of Mines]

## Heat Capacities and Dissociation Equilibria of Gases ${ }^{1}$

By Bernard Lefis ${ }^{2}$ and Guenther von Elbe ${ }^{3}$

Although accurate band spectroscopic data of heat capacities and dissociation equilibria of many gases have been made available during the past four years, we have noted that even in very recent publications the earlier approximate data are still used. In the course of our investigations on gas explosions we have gathered the above data which are available to the present time. We therefore present the following tables, which we hope will be useful to the numerous investigators in this field.

Following the custom adopted by the investigators mentioned below Lewis and Randall's system of symbols will be used.

$$
E_{T}^{\circ}-E_{0}^{\circ}=\int^{T} C_{v} \mathrm{~d} T
$$

The equilibrium constant $K$ for the reaction

$$
A+B \rightleftharpoons A B
$$

is given by

$$
K=p_{\mathrm{A}} p_{\mathrm{B}} / p_{\mathrm{AB}}
$$

where the partial pressures $p_{A}$, etc., are in atmospheres.

Table I

| Energy Content ( $E_{T}^{\circ}-E_{0}^{\circ}$ ) of Gases |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $T_{\mathrm{oemp}_{\mathbf{K}} \mathbf{K}_{\text {p. }}}$ | $\mathrm{H}_{2}$ | $\mathrm{O}_{2}$ | N 2 | CO | NO | $\begin{aligned} & \text { Gas } \\ & \mathrm{OH} \end{aligned}$ | $\mathrm{CO}_{2}$ | $\mathrm{H}_{2} \mathrm{O}$ | O\% | Br 2 | HBr |
| 200 | 965 | 995 | 992 | 992 | 1095 |  |  | 1192 | 1229 | 1134 | 994 |
| 250 | 1197 |  |  |  |  |  |  |  |  | 1454 | 1243 |
| 300 | 1440 | 1492 | 1489 | 1489 | 1616 | 1523 | 1660 | 1791 | 1950 | 1783 | 1493 |
| 400 | 1936 | 2004 | 1987 | 1989 | 2132 | 2034 | 3403 | 2409 | 2786 | 2456 | 1991 |
| 500 |  |  |  |  |  |  |  |  | 3660 | 3140 | 2493 |
| 600 | 2936 | 3086 | 3006 | 3017 | 3196 | 3048 | 4135 | 3687 | 4627 | 3830 | 3003 |
| 700 |  |  |  |  |  |  |  |  | 5644 | 4524 | 3525 |
| 800 | 3947 | 4262 | 4080 | 4112 | 4332 | 4069 | 6107 | 5073 | 6702 | 5222 | 4061 |
| 900 |  |  |  |  |  |  |  |  | 7793 | 5923 | 4612 |
| 1000 | 4979 | 5509 | 5217 | 5271 | 5534 | 5118 | 8246 | 6577 | 8809 | 6626 | 5179 |
| 1200 | 6044 | 6814 | 6442 | 6487 | 6786 | 6200 | 10500 | 8200 |  | 8037 | 6355 |
| 1400 | 7155 | 8150 | 7659 | 7749 | 8074 | 7330 | 12840 | 9920 |  | 9455 | 7579 |
| 1600 | 8295 | 9514 | 8920 | 9045 | 9389 | 8525 | 15220 | 11750 |  | 10880 | 8843 |
| 1800 | 9478 | 10920 | 10220 | 10355 | 10724 | 9740 | 17680 | 13670 |  |  |  |
| 2000 | 10702 | 12352 | 11533 | 11070 | 12073 | 10990 | 20180 | 15650 |  |  |  |
| 2200 | 11945 | 13815 | 12860 | 13007 | 13439 | 12255 | 22680 | 17710 | $\cdots$ | . |  |
| 2400 | 13233 | 15314 | 14199 | 14354 | 14814 | 13565 | 25240 | 19780 |  |  |  |
| 2600 | 14554 | 16825 | 15554 | 15732 | 16197 | 14890 | 27830 | 21930 |  |  |  |
| 2800 | 15894 | 18350 | 16926 | 17110 | 17588 | 16250 | 30450 | 24150 |  |  |  |
| 3000 | 17234 | 19887 | 18295 | 18484 | 18985 | 17607 | 33000 | 26330 |  |  |  |
| 3200 | 18586 | 21415 | 19672 | 19923 | 20387 | 19000 | .. | .. | $\cdots$ |  |  |
| 3500 | 20654 | 23700 | 21747 | 21951 | 22500 | 21105 |  |  |  |  |  |

## Sources of Data

$\mathrm{H}_{2}$ : $E^{\circ}-E_{0}^{\circ}$; Davis and Johnston, This Journal, 56, 1045 (1934).

[^0]$K$; Giauque, ibid., 52, 4816 (1930); Davis and Johnston give slight corrections to Giauque's free energy of $\mathrm{H}_{2}$ above $2000^{\circ}$. The uncertainty in $\Delta E_{0}^{\circ}$ makes it unnecessary to consider these corrections at present.
$\mathrm{O}_{2}: E^{\circ}-E_{0}^{\circ}$ and $K$; Johnston and Walker, ibid., 55, 172, 187 (1933); Lewis and von Elbe, ibid., 55, 507, 511 (1933). The values given in the tables are those of Lewis and von Elbe, which include the contribution of the oxygen ${ }^{1} \Delta$ level.
$\mathrm{N}_{2}: \quad E^{\circ}-E_{0}^{\circ}$; Johnston and Davis, ibid., 56, 271 (1934).
$K$; calculated from fundamental equation $R \ln K$ $=-\Delta\left(F^{\circ}-E_{0}^{0}\right) / T-\Delta E_{0}^{0} / T$ using free energies of N and $\mathrm{N}_{2}$ [Giauque and Clayton, ibid., 55, 4875 (1933)] and $\Delta E_{0}^{\circ}=168,000 \mathrm{cal}$. [Mulliken, Phys. Rev., 46, 144 (1934); also Kaplan, ibid., 45, 898 (1934); Lozier, ibid., 45, 840 (1934); Herzberg and Sponer, Z. physik. Chem., B26, 1 (1934)].
CO: $E^{\circ}-E_{0}^{0}$; Johnston and Davis, loc. cit.
$\left.K_{\left(C+1 / 2 O_{2}\right.}^{\sim}{ }^{2}\right)$; Clayton and Giauque, This Journal, 54, 2610 (1932); corrections are applied to their values to include the oxygen ${ }^{1} \Delta$ level.
NO: $E^{\circ}-E_{0}^{\circ}$; Johnston and Chapman, ibid., 55, 155 (1933).
$\left.K_{(N+}+\mathrm{O} \rightleftharpoons \mathrm{NO}\right) ;$ calculated from fundamental equation $R \ln K=-\Delta\left(F^{\circ}-E_{0}^{0}\right) / T-$ $\Delta E_{0}^{\circ} / T$ using free energy of $O$ (Johnston and Walker, loc. cit.), free energy of N (Giauque and Clayton, loc. cit.), free energy of NO (Johnston and Chapman, loc. cit.) and $\Delta E_{0}^{\circ}=121,000$ cal. (Mulliken, loc. cit.).
$K$ (NO $\left.\rightleftharpoons 1 / 2 \mathrm{O}_{2}+1 / 2 \mathrm{~N}_{2}\right)$; Giauque and Clayton, loc. cit.
$\mathrm{H}_{2} \mathrm{O}: E^{\circ}-E_{0}^{\circ}$; Gordon, J. Chem. Phys, 2, 65, 549 (1934).
$K\left(\mathrm{H}_{\mathbf{3}}+1 / 3 \mathrm{O}_{4} \rightleftharpoons \mathrm{H}_{2} \mathrm{O}\right)$; calculated from fundamental equation $R \ln K=$ $-\Delta\left(F^{\circ}-E_{0}^{\circ}\right) / T-\Delta E_{0}^{\circ} / T$ using free energy of $\mathrm{H}_{2}$ (Giauque, loc. cit.), free energy of $\mathrm{O}_{2}$ (Johnston and Walker, loc. cit.) corrected for ${ }^{1} \Delta$ level, free energy of $\mathrm{H}_{2} \mathrm{O}$ (Gordon, loc. cit.) and $\Delta E_{0}^{\circ}=57,111$ cal. [Rossini, Bur. Stand. J. Res., 6, 1 (1931)].
$K\left(\mathrm{OH}+1 / 2 \mathrm{H}_{8} \rightleftharpoons \mathrm{H}_{2} \mathrm{O}\right)$; calculated from fundamental equation (above) using free energy of OH [Johnston and Dawson, This Journal, 55, 2744 (1933)], free energy of $\mathrm{H}_{2}$ (Giauque, loc. cit.), free energy of $\mathrm{H}_{2} \mathrm{O}$ (Gordon, loc. cit.) and $\Delta E_{0}^{\circ}=63,000$ cal. [Lewis and von Elbe, J. Chem. Phys., 3, 63 (1935)].
$\mathrm{CO}_{2}$ : $E^{\circ}-E_{0}^{\circ}$; Kassel, This Journal, 56, 1838 (1934).
$K\left(\mathrm{CO}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{CO}_{2}+\mathrm{H}_{2}\right)$; calculated from fundamental equation (above) using free energy of CO (Clayton and Giauque, loc. cit.), free energy of $\mathrm{H}_{2} \mathrm{O}$ (Gordon, loc. cit.), frec energy of $\mathrm{CO}_{2}$ (Kassel,

Table II

| uilibrium Constan $\text { Temp., }{ }^{\circ} \mathrm{K} . . . . . .$ | $\text { . } 300$ | $400$ | $600$ | $800$ | $1000$ | $1200$ | $1400$ | $1600$ | 1800 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2 \mathrm{H} \rightleftharpoons \mathrm{H}_{2}+102,800$ | -70.9 | -52.1 | -32.2 | -21.7 | -17.19 | $-13.19$ | $-10.52$ | $-8.48$ | $-6.85$ |
| $2 \mathrm{O} \rightleftharpoons \mathrm{O}_{2}+117,300$ | -80.2 | -58.6 | -36.9 | -26.1 | -19.48 | $-15.10$ | $-11.97$ | $-9.61$ | $-7.772$ |
| $2 \mathrm{~N} \rightleftharpoons \mathrm{~N}_{2}+168,000$ | -117.2 | -86.2 | -55.4 | -39.9 | $-30.6$ | -24.4 | -19.9 | $-16.6$ | -13.9 |
| $2 \mathrm{Cl} \rightleftharpoons \mathrm{Cl}_{2}+56,900$ | -36.43 | -25.91 | $-15.32$ | $-9.99$ | $-6.77$ | $-4.61$ | $-3.06$ | $-1.89$ | $-0.977$ |
| $\underset{66,757}{\mathrm{CO}+1 / 2 \mathrm{O}_{2} \rightleftharpoons \mathrm{CO}_{2}+}$ | $-44.72$ | -32.43 | $-20.07$ | $-13.89$ | $-10.20$ | $-7.755$ | $-5.999$ | $-4.715$ | -3.690 |
| $\begin{aligned} & \mathrm{H}_{2}+1 / 2 \mathrm{O}_{2} \rightleftharpoons \mathrm{H}_{2} \mathrm{O}+ \\ & 6,111 \end{aligned}$ | -39.77 | $-29.26$ | -18.64 | $-13.28$ | $-10.05$ | -7.9() | $-6.34$ | $-5.20$ | $-4.27$ |
| $\underset{63,000}{\mathrm{OH}+1 / 2 \mathrm{H}_{2} \rightleftharpoons \mathrm{H}_{2} \mathrm{O}+}$ | -4:3.3 | -31.7 | -20.0 | $-14.07$ | $-10.53$ | $-8.17$ | $-6.47$ | $-3.20$ | $-4.19$ |

$\mathrm{CO}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{CO}_{2}+\quad-4.947-3.167-1.433-0.610-0.147+0.145+0.341+0.485+0.580$
$\mathrm{H}_{2}+9646$


$\mathrm{O}_{3} \rightleftharpoons 11 / 2 \mathrm{O}_{2}+34,513$| -24.08 | -19.23 | -14.41 | -11.98 | -10.52 | -9.530 | $-8.817-8.277$ | -7.850 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$\mathrm{O}_{2}+\mathrm{O} \rightleftharpoons \mathrm{O}_{3}+24,137-11.83-7.16-2.48-0.13+1.29+2.24+2.92+3.42+3.82$
$\mathrm{NO} \underset{21,400}{\rightleftharpoons} 1 / 2 \mathrm{O}_{2}+1 / 2 \mathrm{~N}_{2}+\quad-15.04-11.13-7.194-5.231-4.052-3.267-2.706-2.285-1.959$

$$
\mathrm{N}+\mathrm{O} \rightleftharpoons \mathrm{NO}+121,000-83.4 \quad-61.2 \quad-38.9 \quad-27.7 \quad-20.93 \quad-16.42 \quad-13.18-10.76
$$

$$
1 / 2 \mathrm{H}_{2}+1 / 2 \mathrm{Cl}_{2} \rightleftharpoons \mathrm{HCl}+
$$

$$
21,984-16.57-12.55-8.52-6.49-5.26-4.44-3.85-3.40-3.06
$$

$$
2 \mathrm{Br} \rightleftharpoons \mathrm{Br}_{2}+45,230 \quad-28.00-19.61-11.21-6.99-4.45-2.74-1.52-0.593 \quad \ldots \ldots
$$

$$
1 / 2 \mathrm{Br}_{2}+1 / 2 \mathrm{H}_{2} \rightleftharpoons \mathrm{HBr}+
$$

$$
11,990
$$

$$
\begin{array}{ccccccccc}
-9.37 & -7.16 & -4.93 & -3.80 & -3.11 & -2.65 & -2.32-2.07 & \ldots \\
2200 & 2400 & 2600 & 2800 & 3000 & 3200 & 3500 & 4000 & 5000
\end{array}
$$

| Temp., ${ }^{\circ} \mathrm{K} . . . . . . . .2000$ | 2200 | 2400 | 2600 | 2800 | 3000 | 3200 | 3500 | 4000 | 5000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2 \mathrm{H} \underset{102,800}{\rightleftharpoons} \mathrm{H}_{2}+\quad-5.53$ | -4.46 | -3.57 | $-2.80$ | $-2.13$ | $-1.58$ | -1.08 | $-0.434+$ | 0.43 | $+1.64$ |
| $2 \mathrm{O} \underset{117,300}{\rightleftharpoons} \mathrm{O}_{2}+\quad-6.298$ | -5.091 | -4.078 | -3.228 | $-2.495$ | -1.858 | $-1.290$ | $-0.577+$ | 0.379 | $+2.715$ |
| $\underset{168,000}{\rightleftharpoons} \mathrm{~N}_{2}+\quad-11.9$ | -10.2 | $-8.72$ | $-7.50$ | $-6.47$ | $-5.56$ | $-4.77$ | - 3.76- | 2.39 | $-0.472$ |
| $2 \mathrm{Cl} \underset{56,900}{\rightleftharpoons} \mathrm{Cl}_{2}+\quad-0.245$ | +0.356 | +0.858 | +1.283 | $+1.648$ | +1.965 |  |  |  |  |
| $\begin{aligned} & \mathrm{CO}+1 / 2 \mathrm{O}_{2} \rightleftharpoons \\ & \mathrm{CO}_{2}+66,757 \end{aligned}$ | -2.193 | $-1.648$ | $-1.20$ | -0.811 | -0.470 |  |  |  |  |
| $\begin{aligned} \mathrm{H}_{2}+1 / 2 \mathrm{O}_{2} \rightleftharpoons & \\ \mathrm{H}_{2} \mathrm{O}+57,111 & -3.52 \end{aligned}$ | -2.91 | -2.41 | -2.00 | $-1.63$ | -1.31 |  | . . . . | . . $\cdot$ |  |
| $\begin{aligned} & \mathrm{OH}+1 / 2 \mathrm{H}_{2} \rightleftharpoons \\ & \mathrm{H}_{2} \mathrm{O}+63,00 \mathrm{O} \\ & \hline \end{aligned}$ | $-2.74$ | -2.19 | $-1.74$ | -1.34 | -0.999 |  |  |  |  |
| $\begin{gathered} \mathrm{CO}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{CO}_{2}+ \\ \mathrm{H}_{2}+9646 \\ +0.658 \end{gathered}$ | $+0.717$ | +0.762 | +0.794 | +0.819 | $+0.840$ |  |  |  |  |
| $\begin{gathered} \mathrm{C}(\beta \text {-graphite })+1 / 2 \mathrm{O}_{2} \rightleftharpoons \\ \mathrm{CO}+27,404 \quad-7.504 \end{gathered}$ | -7.221 | $-6.980$ | $-6.777$ | $-6.595$ | -6.440 |  |  |  |  |
| $\mathrm{O}_{3} \underset{34,513}{\rightleftharpoons} 11 / 2 \mathrm{O}_{2}+\underset{-7.29}{ }$ | $-6.95$ | -6.66 | -6. 42 | -6.21 | -6.03 | $-5.87$ | -5.68- | 5.40 | $-5.02$ |
| $\mathrm{O}_{2}+\mathrm{O}_{24,137} \rightleftharpoons \mathrm{O}_{3}+{ }_{+4.15}$ | +4.41 | +4.63 | +4.81 | $+4.97$ | +5.11 | $+5.23$ | $+5.39+$ | 5.60 | $+5.89$ |
| $\begin{aligned} & \mathrm{NO} \underset{1 / 2}{\rightleftharpoons} \mathrm{~N}_{2}+21,400-1,695 \end{aligned}$ | -1.479 | $-1.300$ | $-1.150$ | $-1.019$ | $-0.907$ | $-0.807$ | - $0.680-$ | 0.513 | $-0.279$ |
| $\underset{121,000}{ } \underset{-7.35}{ }$ | $-6.11$ | $-5.065$ | -4.194 | $-3.431$ | $-2.778$ | -2.203 | - 1.465- | 0.475 | + 0.924 |
| $\begin{aligned} & 1 / 2 \mathrm{H}_{2}+1 / 2 \mathrm{Cl} \stackrel{\rightleftharpoons}{\mathrm{HCl}+21,984-2.78} \end{aligned}$ | $-2.55$ | $-2.36$ | $-2.20$ | -2.06 | $-1.94$ | . . . . |  |  |  |

loc. cit.; Gordon, J. Chem. Phys., 1, 308 (1933), up to $1500^{\circ} \mathrm{K}$.), free energy of $\mathrm{H}_{2}$ (Giauque, loc. cit.) and $\Delta E_{0}^{\circ}=9646$ (from Rossini's thernal data, Bur. Stand. J. Res., 6, 37 (1931)).
$K\left(\mathrm{CO}+1 / 3 \mathrm{O}_{2} \rightleftharpoons \mathrm{CO}_{2}\right)$; calculated by multiplying

$\mathrm{O}_{3}: E^{\circ}-E_{0}^{\circ}$; calculated from Gerhard's [Phys. Rev., 42, 622 (1932)] fundamental frequencies 528,1033 and $1355 \mathrm{~cm} .^{-1}$, with anharmonicity corrections, estimated by Kassel (private communication).

$\mathrm{OH}: E^{\circ}-E_{0}^{\circ}$; Johnston and Dawson, loc. cit.

$\mathrm{Br}_{2}$ : $E^{\circ}-E_{0}^{\circ}$ and $K$; Gordon and Barnes, J. Chem. $\mathrm{HBr}: E^{\circ}-E_{0}^{\circ}$ and $K$; $\}$ Phys., 1, 693 (1933).

## Summary

Accurate data of heat capacities and dissociation
equilibria derived from band spectroscopic data of gases have been gathered and arranged in two tables. Table I contains the energy content of $\mathrm{H}_{2}, \mathrm{O}_{2}, \mathrm{~N}_{2}, \mathrm{CO}, \mathrm{NO}, \mathrm{OH}, \mathrm{CO}_{2}, \mathrm{H}_{2} \mathrm{O}, \mathrm{O}_{3}, \mathrm{Br}_{2}$ and HBr from 200 to $3500^{\circ} \mathrm{K}$.; Table II contains equilibrium constants of numerous equilibria involving these gases and also $\mathrm{Cl}_{2}$ and HCl from 300 to $5000^{\circ} \mathrm{K}$. Complete references to sources of data are given.
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# The Reactions Taking Place in the Iodimetric Determination of Chromates 

By Friedrich L. Hahn

It has been known for a long time that in the iodimetric titration of chromates an excess of thiosulfate is often consumed. ${ }^{1}$ This has been attributed to an air oxidation of the iodide in acid medium. However, this explanation does not account fully for the various phenomena observed in the system dichromate-acid-iodidethiosulfate. The excess in the quantity of thiosulfate required in feebly acid solutions cannot be caused by the action of atmospheric oxygen, because it is large in a rapid determination, diminishes as one prolongs the titration and disappears when some time is allowed to elapse, after having acidulated the solution before beginning the titration (Kolthoff).

The author has found that the various phenomena observed can be explained by the formation of a complex between chromic chromium and thiosulfate, this complex reacting only very slowly with iodine. ${ }^{2}$ Chromic chromium once formed does not react with the thiosulfate, but the complex is formed when the reduction of chromate takes place in the presence of thiosulfate. This hypothesis enables us to predict phenomena verifiable by experiment.
I. If the excess of reagent consumed for feebly acid solutions is not due to an excessive formation of iodine but to an irregular fixation of the thiosulfate, it must be specific for thiosulfate as reducing agent and it ought to disappear, if the liberated iodine is reduced by another reagent; this
(1) G. Bruhns, Z. anorg. allgem. Chem., 49, 277 (1916); J. prakt. Chem., 98, 73, 312 (1916): 95, 37 (1917): I. M. Kolthoff, Z. anal. Chem., 59, 401 (1920). Later investigations concerning the same subject, e. g., K. and W. Böttger, ibid., 69, 145 (1926). or A. Friedrich and E. Bauer, ibid., 97, 305 (1934), have not contributed to solution of the problem in question.
(2) Preliminary pablication, Z. anal. Chem., 97, 305 (1934).
was found on titrating the iodine with stannous chloride.
II. If the excess of thiosulfate fixed into the complex reacts slowly with iodine, the theoretical quantity of iodine will be found on titrating the colorless final solution drop by drop with iodine until the iodine color is definitively stable and by subtracting this quantity of iodine from the quantity of thiosulfate consumed. This is proved by experiments.
III. The smallest traces of thiosulfate may be detected by the catalysis of a mixture of sodium azide $\left(\mathrm{NaN}_{3}\right)$ and iodine, decolorizing the iodine and forming gaseous nitrogen. ${ }^{3}$ This reaction reveals the presence of thiosulfate in the end solutions, although containing free iodine, of titrations in which an excess of thiosulfate has been used; this thiosulfate is furnished by decomposition of the thiosulfate-chromic complex. The reaction does not take place in solutions from exact titrations.
IV. The quantity of the complex formed in a titration ought to increase with the quantity of chromate present during the addition of the thiosulfate, and this diminishes with the concentration of $\mathrm{H}^{+}$or $\mathrm{I}^{-}$ions increasing. This is in agreement with the fact that the excess of thiosulfate diminishes when the acidity of the solution increases; one may anticipate that for solutions of the same concentration in acid an increase of iodide will also diminish the thiosulfate required. This also is verified by experiment (Trials a and e, $b$ and $f$ on Table I).
V. Regarding quantitative relations it may be anticipated that the reactions on the sodium azide
(3) Reaction investigated by Fr. Feigi, ibid., T6. 376 (1928).


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